



# Using Machine Learning, Business Rules, and Optimization for Flash Sale Pricing

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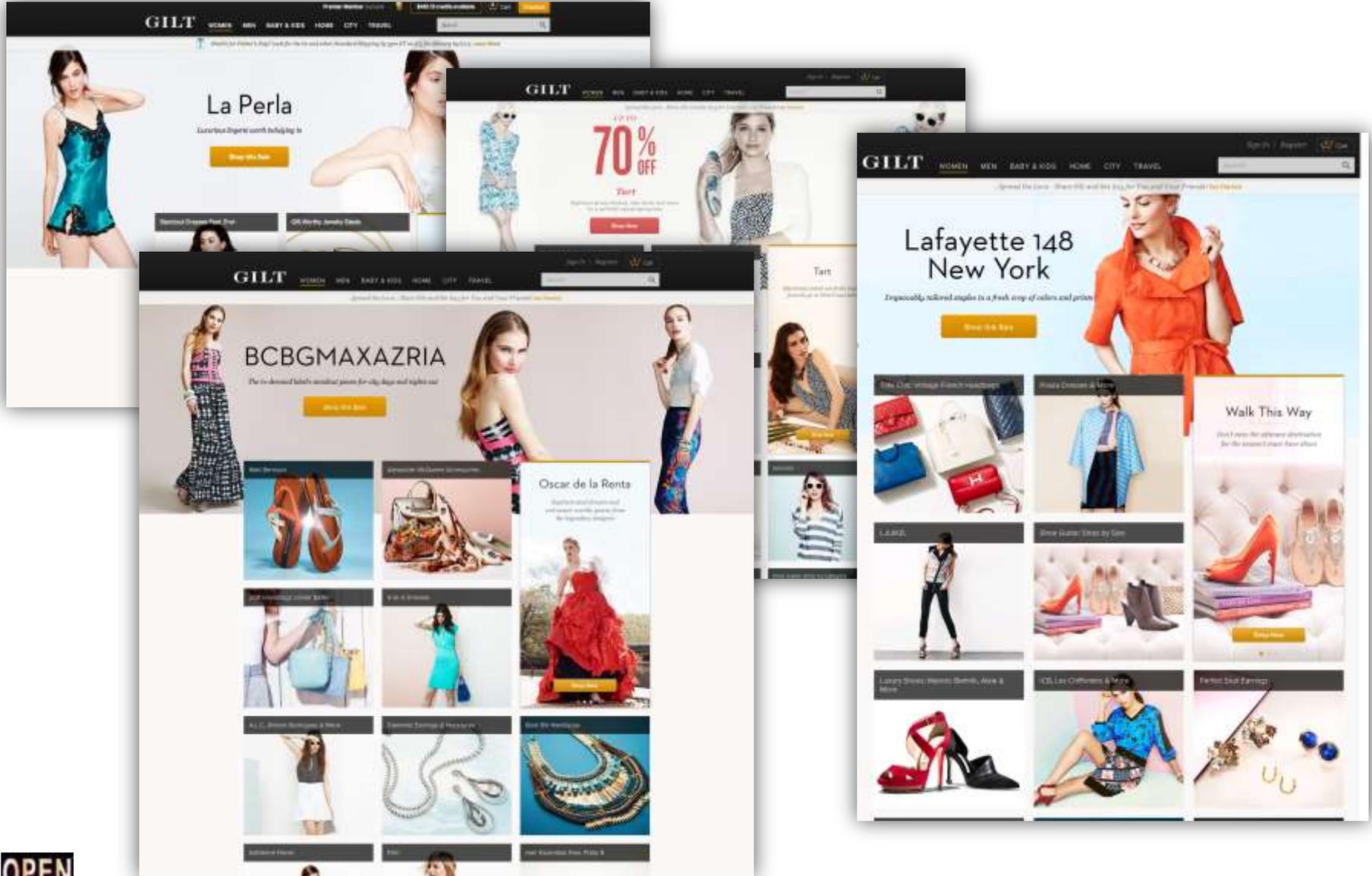
- GILT:
  - Online retailer selling curated collections of fashion products via flash sales
- Expected Functionality:
  - Utilize sales history to predict demand for ever-changing assortments of thousands of products
  - Collaborate with business domain experts to quickly generate optimal prices that can immediately go live on site

- A combination of Machine Learning, Business Rules, and Multi-Objective Optimization:
  - Predictive Analytics
    - R, xgboost
  - Business Rules
    - OpenRules
  - Optimization
    - OpenRules/JSR-331 with various linear solvers

# Before Gilt – sample sales



# Gilt pioneered online “flash sales” in US



# LIFESTYLE MARKETING PLATFORM

Gilt is a members-only lifestyle destination and ecommerce site that provides insider access to today's top designer brands as well as exclusive local experiences.



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**9.7M+**

active members

**400**

sales launch weekly

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**7K+**

packages shipped daily

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**100**

countries shipped to

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**1M+**

active mobile app users\*

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**50%**

of revenue is generated via mobile purchases

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**1B+**

highest press impressions from a single partnership\*\*

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**1.5M+**

social media followers



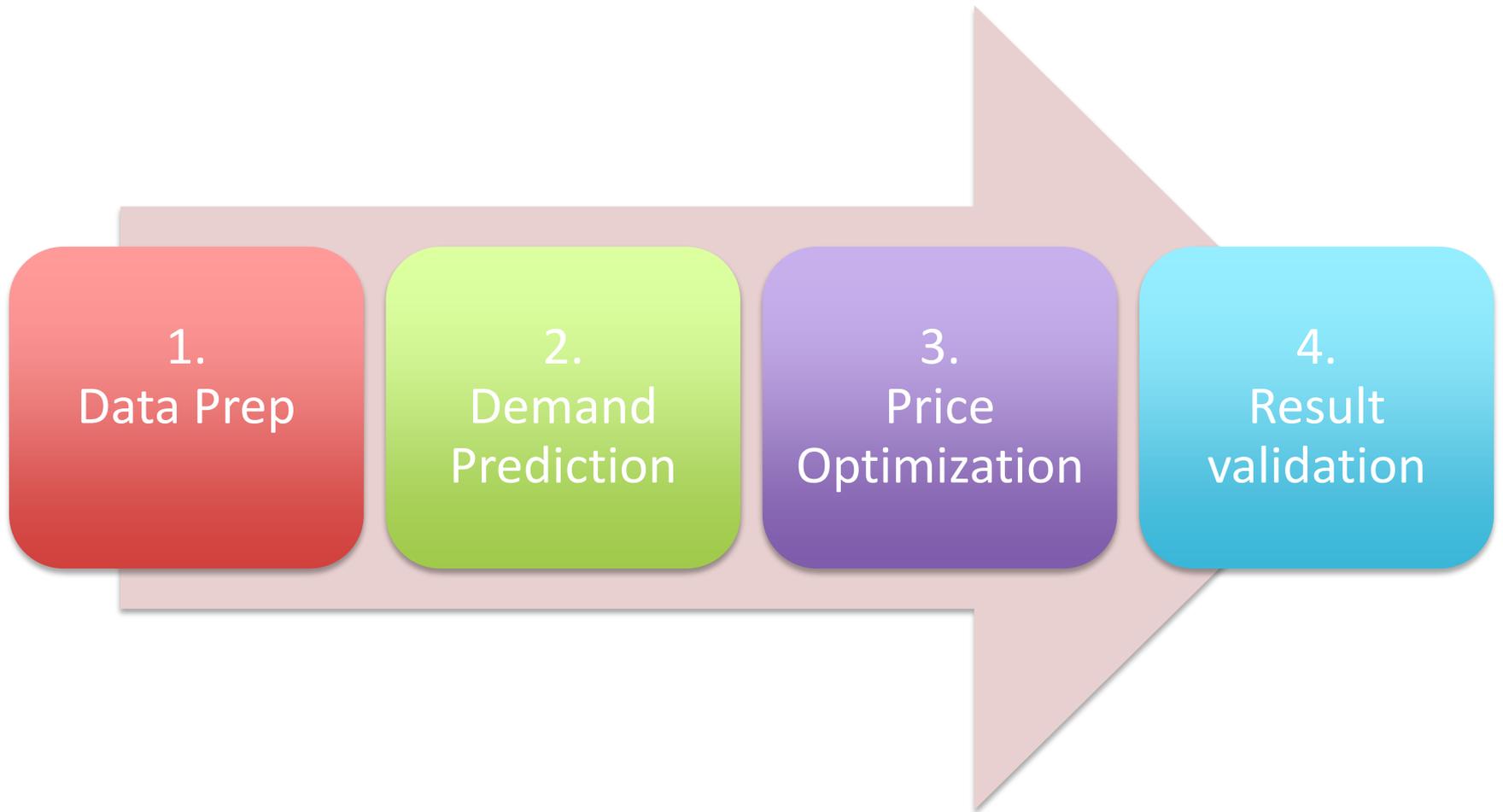
# How to price thousands of items every day?

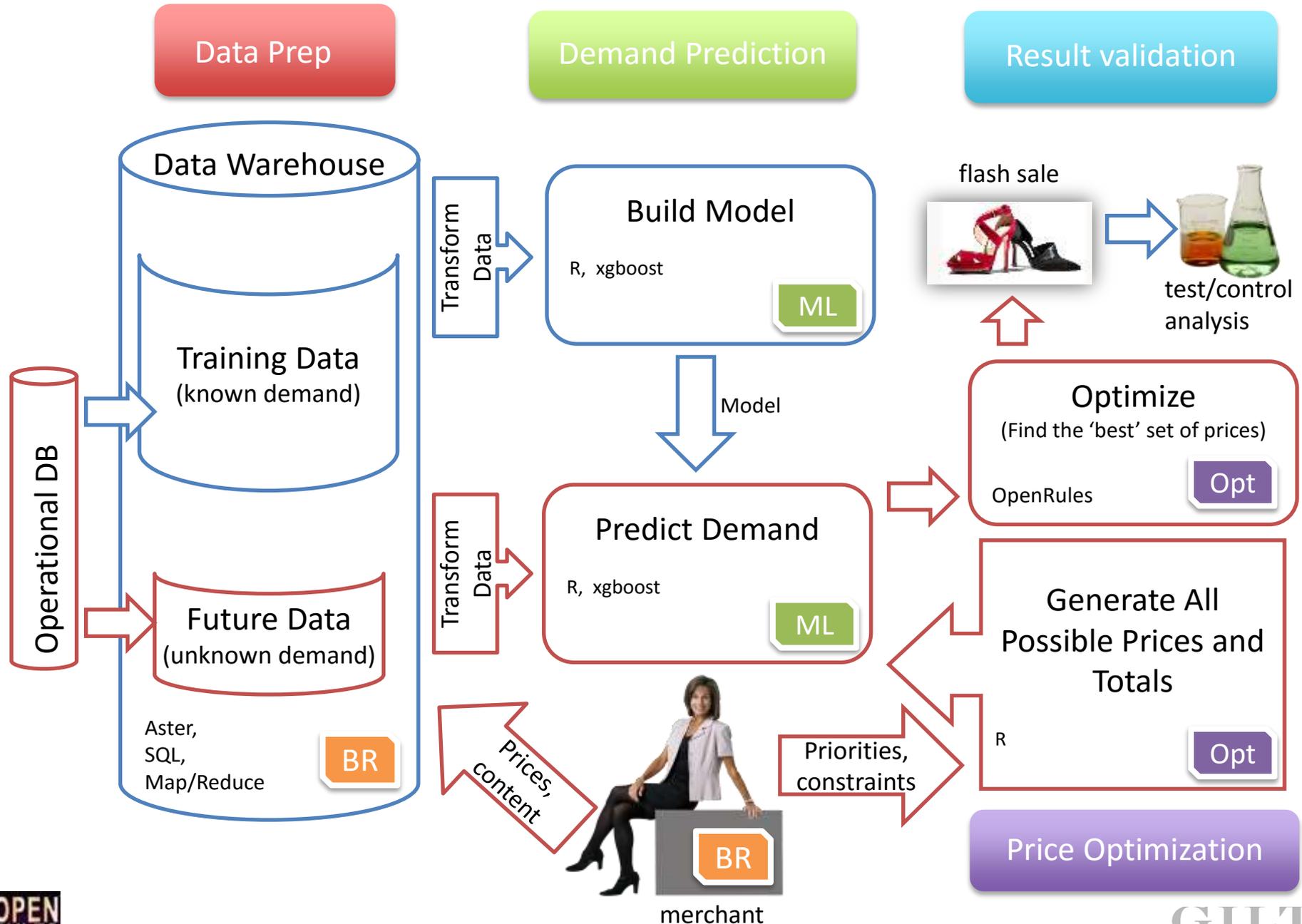
 <p>Sergio Rossi Secret Pointed-Toe Pump #1299 <del>\$349</del></p>	 <p>PURE NAVY Pointed-Toe Pump #999 <del>\$89</del></p>	 <p>Furla Giselle Pointed-Toe Pump #1250 <del>\$249</del></p>
<p>2 Left</p>  <p>Aperil Leather Fringed Pump #12388 <del>\$449</del></p>	 <p>Maiden Lane Classic Leather Pointed-Toe Pump #699 <del>\$79</del></p>	 <p>Corso Como Wellsley Laser-Cut Leather Pump #1259 <del>\$89</del></p>
<p>2 Left</p>  <p>Giuseppe Zanotti Pointed-Toe Pump #12991 <del>\$279</del></p>	 <p>Sergio Rossi Godiva Leather Pointed-Toe Pump #12623 <del>\$299</del></p>	 <p>Corso Como Wellsley Laser-Cut Leather Pump #1259 <del>\$89</del></p>



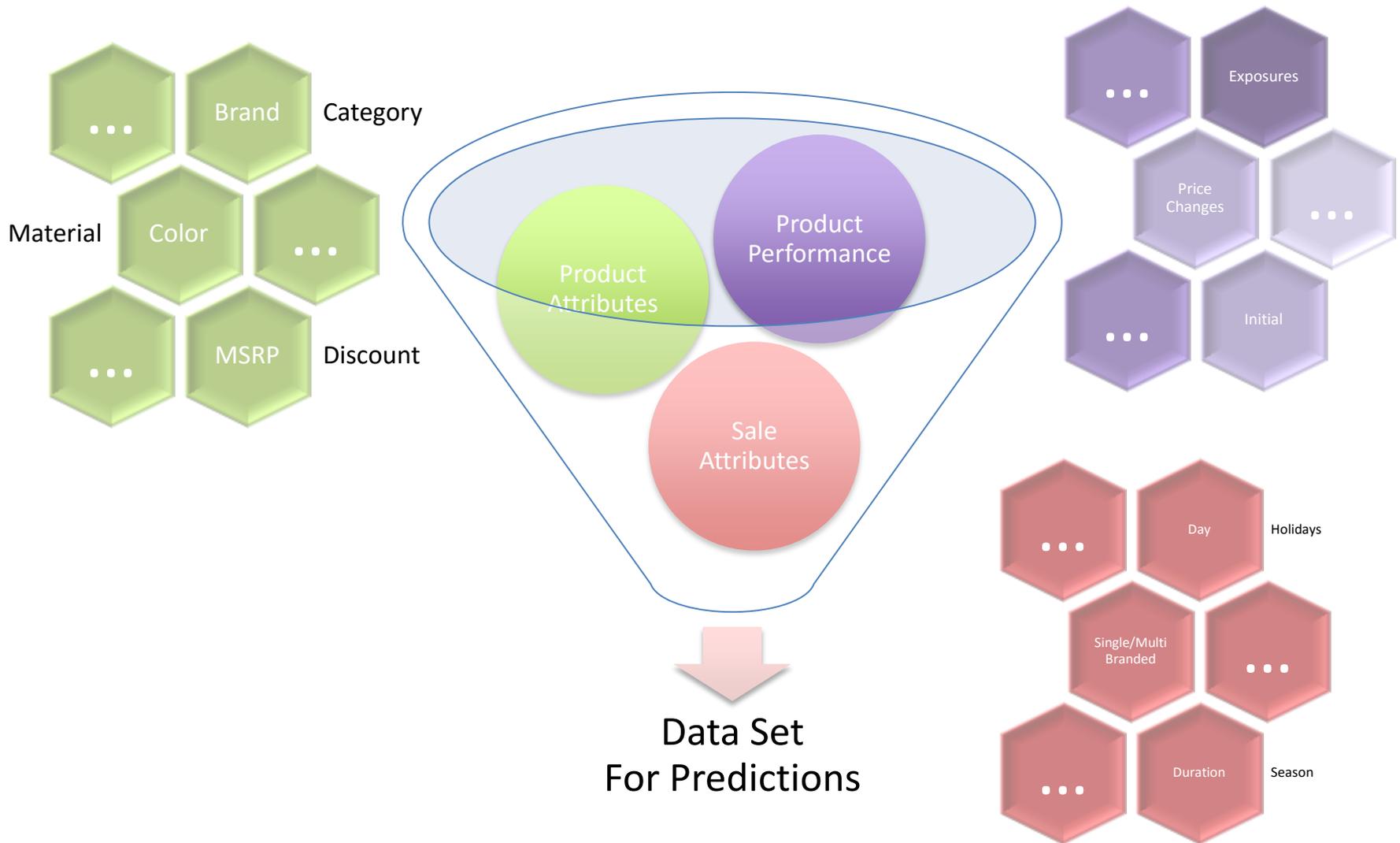
- **Predict demand** for every product in a given sale for all possible prices
- **Find the best combination of prices** to satisfy business objectives (weighted mix of revenue, margin, sell-through, etc)
- **Present** price recommendations to business

# How it's done



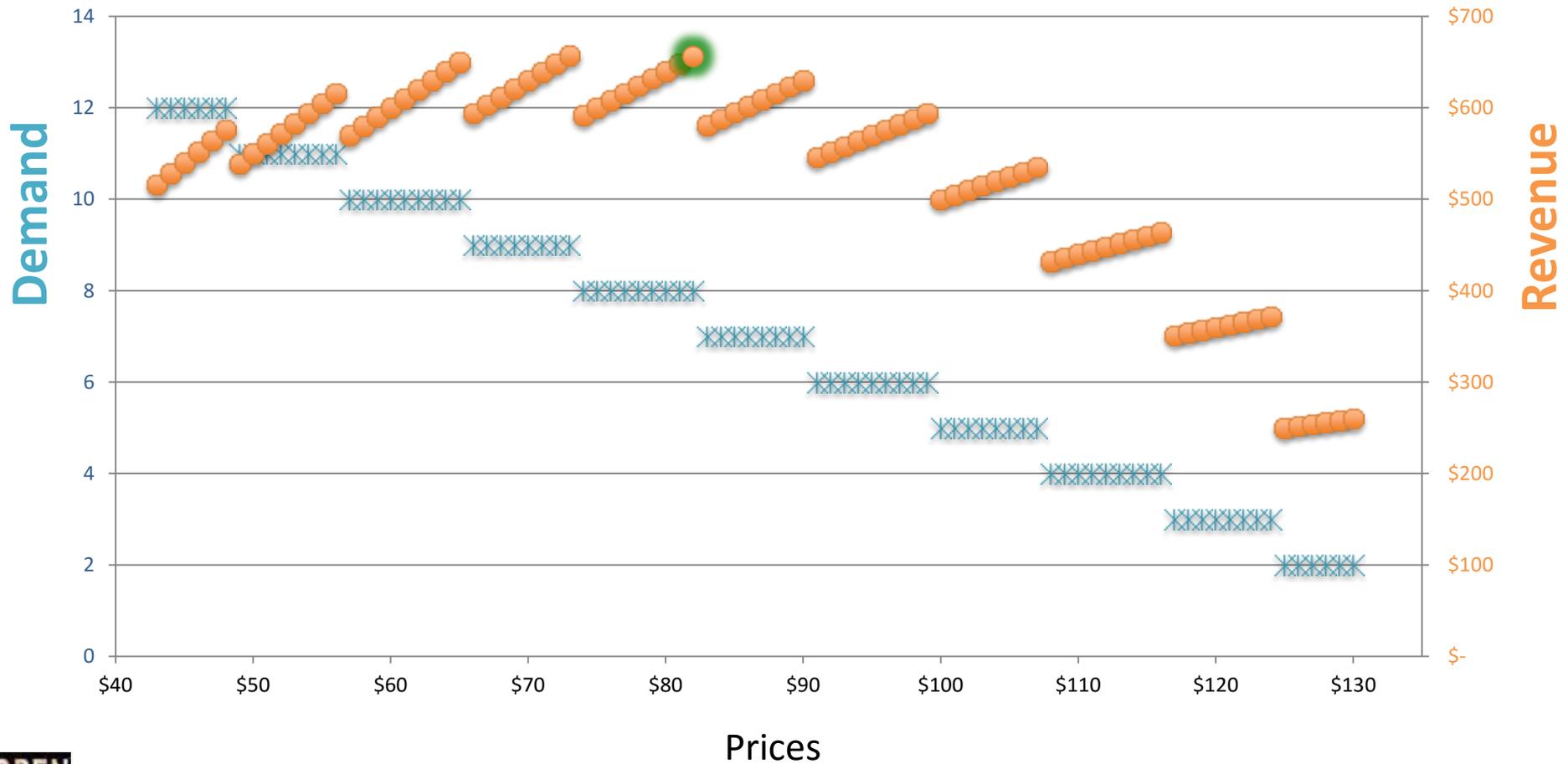


# 1. Data Preparation



# 2. Demand Prediction

Example: Predicted Demand and Revenue at different Prices



# 3. Price Optimization

- Goals:
  - optimize per product and per sale
  - allow business user to set goals (revenue, sell-through, margin, or combination)
- Iterate quickly

# Sample Rules

Minimal Number of Previous Exposures		Variable	<oper>	Value		
Is	0	Minimum Discount from MSRP	Is	20		Initial Sales
Is	0	Percent Difference from Original Price		40		
Is	0	Minimal Margin Percent		40		
Is	0	Minimal Sell Through Percent		20		
Is	1	Minimum Discount from MSRP	Is	20		Repeat Sales
Is	1	Percent Difference from Original Price		40		
Is	1	Minimal Margin Percent		30		
Is	1	Minimal Sell Through Percent		20		
Is	10	Minimum Discount from MSRP	Is	60		Exit Sales
Is	10	Percent Difference from Original Price		40		
Is	10	Minimal Margin Percent		5		
Is	10	Minimal Sell Through Percent		40		

# Optimization Weights

Variable	<oper>	Value
Gross Revenue Weight	Is	2
Gross Margin Weight		5
Gross Sell Through Weight		3

Sample Results For A Sale:

Target	Revenue	Margin	Sell-through
Max Revenue	\$6,606	58%	23%
Max Margin	\$4,289	67%	16%
Max Sell-through	\$5,628	48%	24%

Best predictors of demand (number of units sold):

- Number of units available
- Price, Discount, MSRP
- Item price relative to the prices of other items in the sale
- Product attributes, etc

Prediction changes:

Before: predict demand for all acceptable prices

Now: same as before but **for all possible totals**

## Example



Prices: \$2 or \$4



Prices: \$1 or \$3

Price total: \$3 - \$7

- Apply constraints early
- Calculate all the totals

Item	Price	Total	Demand
<b>Ball</b>	<b>\$2</b>	<b>\$3</b>	<b>4</b>
Ball	\$2	\$4	4
<b>Ball</b>	<b>\$2</b>	<b>\$5</b>	<b>4</b>
Ball	\$2	\$6	3
Ball	\$2	\$7	3
Ball	\$4	\$3	2
Ball	\$4	\$4	2
<b>Ball</b>	<b>\$4</b>	<b>\$5</b>	<b>2</b>
Ball	\$4	\$6	2
<b>Ball</b>	<b>\$4</b>	<b>\$7</b>	<b>2</b>
<b>Pen</b>	<b>\$1</b>	<b>\$3</b>	<b>7</b>
Pen	\$1	\$4	7
<b>Pen</b>	<b>\$1</b>	<b>\$5</b>	<b>8</b>
Pen	\$1	\$6	8
Pen	\$1	\$7	8
Pen	\$3	\$3	1
Pen	\$3	\$4	1
<b>Pen</b>	<b>\$3</b>	<b>\$5</b>	<b>1</b>
Pen	\$3	\$6	1
<b>Pen</b>	<b>\$3</b>	<b>\$7</b>	<b>0</b>

- All items must be priced
- Each item must have only one price
- Sum of all prices should equal to one and only one total

```

set Look;
set Price := 1..10000;
set Total := 1..100000;

set Look_Price_Total within {l in Look, p in Price, t in Total};
param price {(l,p,t) in Look_Price_Total}, >= 0, integer := p;
param demand {Look_Price_Total}, >= 0, integer;
param revenue{(l,p,t) in Look_Price_Total} := price[l,p,t] * demand[l,p,t];

param orig_price {Look_Price_Total}, >= 0, integer, default 0;
param base_price {Look_Price_Total}, >= 0, integer, default 0;
param msrp_price {Look_Price_Total}, >= 0, integer, default 0;
param num_units_available {Look_Price_Total}, >= 0, integer, default 0;

set Unique_Total := setof{(l,p,t) in Look_Price_Total} t;

var Use {Look_Price_Total} binary;
var Use_Total {Unique_Total} binary;

maximize Revenue:  sum{(l,p,t) in Look_Price_Total} revenue[l,p,t] * Use[l,p,t];

s.t. one_of_each{l in Look}: sum{(l,p,t) in Look_Price_Total} Use[l,p,t] = 1;
s.t. single_total: sum{t in Unique_Total} Use_Total[t] = 1;
s.t. price_sum_is_total{t in Unique_Total}:
    sum{(l,p,t) in Look_Price_Total} price[l,p,t] * Use[l,p,t] = t * Use_Total[t];

```

```

set Look := Ball Pen;
param: Look_Price_Total: demand :=
Ball    2    3    4
Ball    2    4    4
Ball    2    5    4
Ball    2    6    3
Ball    2    7    3
Ball    4    3    2
Ball    4    4    2
Ball    4    5    2
Ball    4    6    2
Ball    4    7    2
Pen     1    3    7
Pen     1    4    7
Pen     1    5    8
Pen     1    6    8
Pen     1    7    8
Pen     3    3    1
Pen     3    4    1
Pen     3    5    1
Pen     3    6    1
Pen     3    7    0;

```

- We modeled the problem using OpenRules and JSR-331 Standard
- Real optimization problems consist of hundreds of thousands records:
  - We used JSR-331 Constraint Solvers to validate the problem correctness. But actual problems were too large for constraint solvers
  - We tried various JSR-331 Linear Solvers (GLPK, LP-Solve, COIN suite, SCIP, and others)
  - None was able to solve large problems in a reasonable time or at all

- OpenRules was able to create a rules-based decision model that automatically splits one large problem into a set of smaller sub-problems (one for every individual total cost)
- While there may be thousands of sub-problems, JSR-331 Linear Solvers are able to quickly solve them
- Then OpenRules decision model analyzes all found solutions to come up with the optimal solution that satisfy a configurable combined objective – a maximal combination of Revenue, Margin, and Sell-Through
- Big advantage of this approach: it can be parallelized to solve even much larger problems!

- We applied a combination of Machine Learning, Business Rules, and Multi-Objective Optimization to solve a real-world operational problem – flash sale price optimization
- The pricing methodology and tools that support each of these 3 decision management techniques were readily available and quite powerful
- However, the production-level problems required a special ingenious approach to actually solve these problems

# Questions?



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**GILT**

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